

Forecasting Research

**Forecasting Research Division
Technical Report No. 45**

Running the global wave model with shallow water depth information

by

M.W. Holt

April 1993

**Meteorological Office
London Road
Bracknell
Berkshire
RG12 2SZ
United Kingdom**

Running the global wave model with shallow water depth information.

M W Holt

Forecasting Research Division

Technical Report No. 45

April 1993

**Forecasting Research Division, Meteorological Office,
London Road, Bracknell RG12 2SZ**

**This document has not yet been published. Permission to quote from it
must be obtained from an Assistant Director of the above Division.**

1 Introduction

Forecasts of wave height and direction from the global wave model are used by the Ship's Routing forecasters in CFO to route voyages across the oceans. These are in deep water ($> 200\text{m}$ depth) for most of the time. Forecasts from the global model are also used to provide offshore forecasts for the North Sea after $t+36$ hours. Here, depending on the wavelengths present, the water may be effectively shallow. There is also increasing interest in providing forecast wave data in the South China Sea and the Gulf of Mexico, for the offshore oil industry. These operations are often in areas of 'shallow' water, with depths less than 200m .

The regional wave model run at the UK Met Office already includes the effects of shallow water on the wave spectrum. This note describes the impact of including shallow water effects in the global wave model, at a resolution of 0.833 degrees latitude by 1.25 degrees longitude.

Section 2 of this paper briefly describes the shallow water source terms; Section 3 gives details of the depth dataset used and assesses the likely impact. In Section 4 the results of a parallel run are described, and Sections 5 and 6 summarise and give recommendations for operational implementation.

2 Shallow water source terms

Three separate effects are included when shallow water terms are included in the UK Met Office wave model. These are a) the shallow water group velocity is used, b) bottom friction is accounted for, and c) refraction by the depth gradient is calculated. Full details of the physics of these terms are to be described in a later Technical Note, however brief details are given here.

a) Wave energy is advected with the group velocity, which is a function of wave frequency. For waves in shallow water the group velocity is also a function of depth. Within the wave model, shallow water group velocities are calculated at depth intervals of 1m down to 200m depth. For water of depth 200m or greater the deep water value for group velocity is used.

b) When waves travel into water shallower than about one quarter their wavelength, the wave induced motion at the sea bed becomes significant. The physical effect arising from this depends on the nature of the sea bed, and the different mechanisms are discussed in more detail in Shemdin (1978) (and will be reviewed in a later Technical Note). However the averaged affect of these processes on the wave model grid scale is well represented by a simple expression for the associated sink of wave energy:

$$S_{bf} = - \text{Const } g k^2 \{U\} E(f, \theta) / [2\pi f \cosh(kH)]^2$$

where k is the shallow water wave number, H is the depth, g the acceleration due to gravity, E the wave energy density and $\{U\}$ is the mean orbital velocity at the sea bed of the water in the wave at the sea bed, given by :

$$\{U\}^2 = \iint [gk/2\pi f \cosh(kH)]^2 E df d\theta$$

c) As a wave propagates into shallower water it is refracted by the varying depth gradient. Phase speeds are less in shallow water. Frequency of the wave is conserved, but the wavenumber k is not conserved as the wave moves into shallower water. The shallow water dispersion relationship, $\omega^2 = g k \tanh(kH)$, relates wave frequency to wavenumber and depth. The refraction acts to turn the wave energy but does not alter the frequency or amount of wave energy present. This is why waves generally approach parallel to a beach. The source term is:

$$dE/dt = - d \{ (c_g \cdot \nabla \theta) E \} / d\theta$$

In the UK Met Office wave model the gradients of sea bed topography are calculated using centred differences, with the depth at coast points set to zero. The refraction function is calculated using an upstream difference scheme. Refraction is calculated at all wave model 'sea' points, for frequencies lower than 0.15Hz.

3 Global depth dataset

Depths were taken from a one twelfth degree US Navy dataset, used in the UK Met Office for ocean and climate modelling. The depths were averaged to a half degree grid, and then interpolated onto the wave model grid at 0.833 by 1.25 degrees resolution. The depths in the wave model were not smoothed. No account was taken of tidal or other causes of deviation of the sea surface from the geoid.

Figure 1 shows the depths used in the global wave model. It is clear that the majority of the water is greater than 200m depth, so is 'deep' water for the wave model. There are several important areas with depths less than 200m, shown in Figure 2. These are 2a) the North Sea, 2b) the South China Sea, 2c) the China Sea, 2d) N Australia, and 2e) the Falkland Islands. The Gulf of Mexico (Figure 2f) is mostly greater than 200m depth. However the inclusion of depth information does not necessarily mean that these areas will be 'shallow' water for the range of wavelengths normally present. Figure 3 shows the (approximate) depth in which deep water waves of a given frequency will first feel the sea bed. (The depth plotted is taken as one quarter

the deep water wavelength). Clearly if no waves of this wavelength or longer are present then there will be no impact from including shallow water information at that gridpoint. The effects of shallow water are thus more important for swell than for windsea.

4 Results of a parallel run

The global shallow water version of the wave model has been run in parallel with the operational model for several weeks, starting from 4th March 1993. An assessment of the global coverage of differences in wave height (Figure 4) shows only small differences in mid ocean, with larger differences noticeable in some of the shallow water areas mentioned above. Differences greater than 10cm are shaded.

In the North Sea there are differences of up to 30cm wave height in coastal waters, with a total wave height of 3m to 3.5m (Figure 5a and 5b). There is little difference in the southern North Sea, where wave heights are up to 2.5m. Results from the global shallow water run may be compared with the operational Global and European model output (Figure 6a,b,c). The results show little difference in wave height between all three models under normal circumstances. There is more detail present in the European model, since Orkney and the Shetlands are included and the coastlines are better resolved, giving improved wave heights under fetch limited conditions. When wave heights reach several metres, it is clear that the inclusion of bottom friction in both the global shallow and European model runs reduces the peak wave height by up to 0.5m, from eg 5m to 4.5m. (See for example the maximum wave height south of Ireland in Figure 6). Generally, as wave height increases, the peak of the spectrum moves towards lower frequency, hence longer wavelength. In these cases the global shallow run is closer to the European model than is the global deep water operational.

Differences in wave direction may be seen particularly in the shallower waters of the southern North Sea and at coast points (Figure 7). In deep water there is little or no difference in wave direction between the control and shallow runs. Wave direction is output from the wave model by calculating the components of wave energy at each grid point. Thus all wave energy, even if from more than one separate wave train, is counted. Where more than one wave train is present at a point, the calculated direction can be misleading, and where the relative amplitude of wave systems varies from one point to the next, there can be differences in wave direction at adjacent gridpoints. For example in Figure 7 west of the Hebrides the shallow water version has reduced the amount of swell from the NE at several points, so the direction is predominantly that of the windsea, from the NW, rather than from the NE at these points.

In the South China Sea the differences in wave height are confined close to the coasts and are much smaller than seen in the North Sea (Figure 8). The area is effectively deep water for the waves present. Differences in wave direction may be seen close to the coasts and at coast points, because of refraction effects (Figure 9). These cannot be verified as no observations are available. Here again the shallow run has removed some of the swell energy from the NE so that in the eastern South China Sea the wave direction in the shallow run at several gridpoints follows the windsea, from south of west, different to the operational model which is dominated by swell from the NNE. Although the mean wave directions are different at these points there is negligible difference in wave height.

Similar differences between the shallow and control runs are noticeable in the China Sea and around the Falkland Islands and close to Japan.

COSTS

Estimates of costs for the global model from 6-timestep runs in batch are :

	CPU	elapsed	machine
GLOBAL DEEP	160 sec	28 sec	67% of 8-CPU
GLOBAL SHALLOW	195 sec	45 sec	54% of 8-CPU

An increase of approximately 35 sec CPU (22%) per 6 hours run.

The bulk of the increase comes from calculations performed in the physics subroutine:

PHYSICS costs	CPU	elapsed	% machine
GLOBAL DEEP	79 sec	13 sec	54% of 8-CPU
GLOBAL SHALLOW	101 sec	25 sec	60% of 8-CPU

ADVECTION costs	CPU
GLOBAL DEEP	61.2 sec
GLOBAL SHALLOW	59.9 sec

FILE SIZES

Including depth information does not alter the size of the wave model forecast file. The deep-water file already holds a value of 200m depth at each gridpoint.

5 SUMMARY

There is a clear case dependent improvement from including shallow water physics in the global wave model. Where the waves are in shallow water there is an improvement in modelled wave height. Differences are most noticeable over the N Sea, for wave heights greater than (approx) 2m, and in such cases the global shallow water values are closer to the wave heights from the European wave model. Thus using the global shallow water model would provide a more consistent forecast for Aberdeen Weather Centre. Differences in direction may be seen in shallow water and at coast points, and in open water $< 200\text{m}$ where swell may be reduced thus giving more emphasis to the windsea direction in the calculation of mean wave direction.. These cannot be verified. At the time of the trial there was little impact seen in the South China Sea, the water there is effectively deep for the wavelengths present. Apart from small differences in wave height in the North Sea in moderate sea state, there was no wave height difference at any of the buoy locations used in routine verification of the operational global wave model.

6 RECOMMENDATIONS

- a) The global wave model should be extended to include shallow water effects.
- b) The trial should continue, to assess the impact on swell arriving in the S China Sea from the monsoon or from tropical storms.

REFERENCES:

- | | | |
|----------------|------|---|
| Shendin, O | 1978 | Nonlinear and linear bottom interaction effects in shallow water. in Turbulent Fluxes through the sea surface, wave dynamics and prediction. Plenum Press, pp 347 - 370 |
| Hasselmann, K, | | |
| Hsiao, S V and | | |
| Herterich, K | | |

FIGURES:

Figure 1 Global sea depths. Depths $< 200\text{m}$ are shaded.

Figure 2 Global model depths by region.

- a) The North Sea
- b) The South China Sea
- c) The China Sea
- d) North Australia
- e) The Falkland Islands
- f) The Gulf of Mexico

Shading is light for 0-60m, medium for 60-120m and dark for 120-180m. Contour interval 10m.

Figure 3 Depth at which deep-water waves of a given frequency first feel the sea bed.

Figure 4 Wave height differences Operational minus Shallow. VT 12z 30/3/1993.

Contour interval 10cm, differences $> 10\text{cm}$ shaded.

Figure 5 a) Wave height differences over the North Sea. Shading 0.1-0.2m (light), 0.2-0.3m (medium) and $> 0.3\text{m}$ (dark).

- b) Operational global model wave heights over the N Sea.
Shading 0-3m light, 3-6m medium and $> 6\text{m}$ dark.

Figure 6 a) Operational, b) shallow water and c) European model wave heights over the N Sea. VT 12z 30/3/1993. Shading as Figure 5b

Figure 7 Wave directions over the North Sea. Solid arrows operational, dashed arrows from shallow run.

Figure 8 Wave height differences over the South China Sea. Contour interval 0.1m

Figure 9 Wave directions over the South China Sea

Figure 1

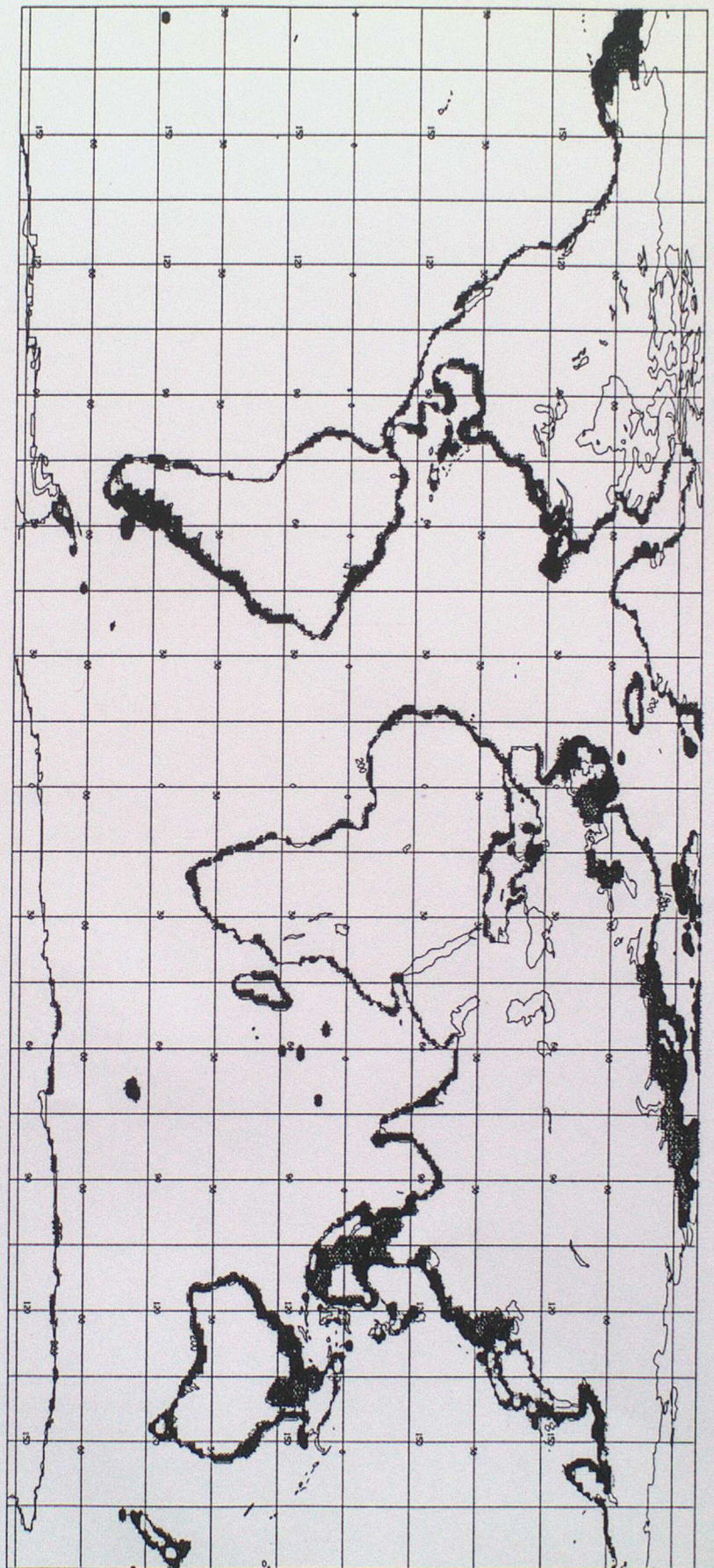


Figure 2a

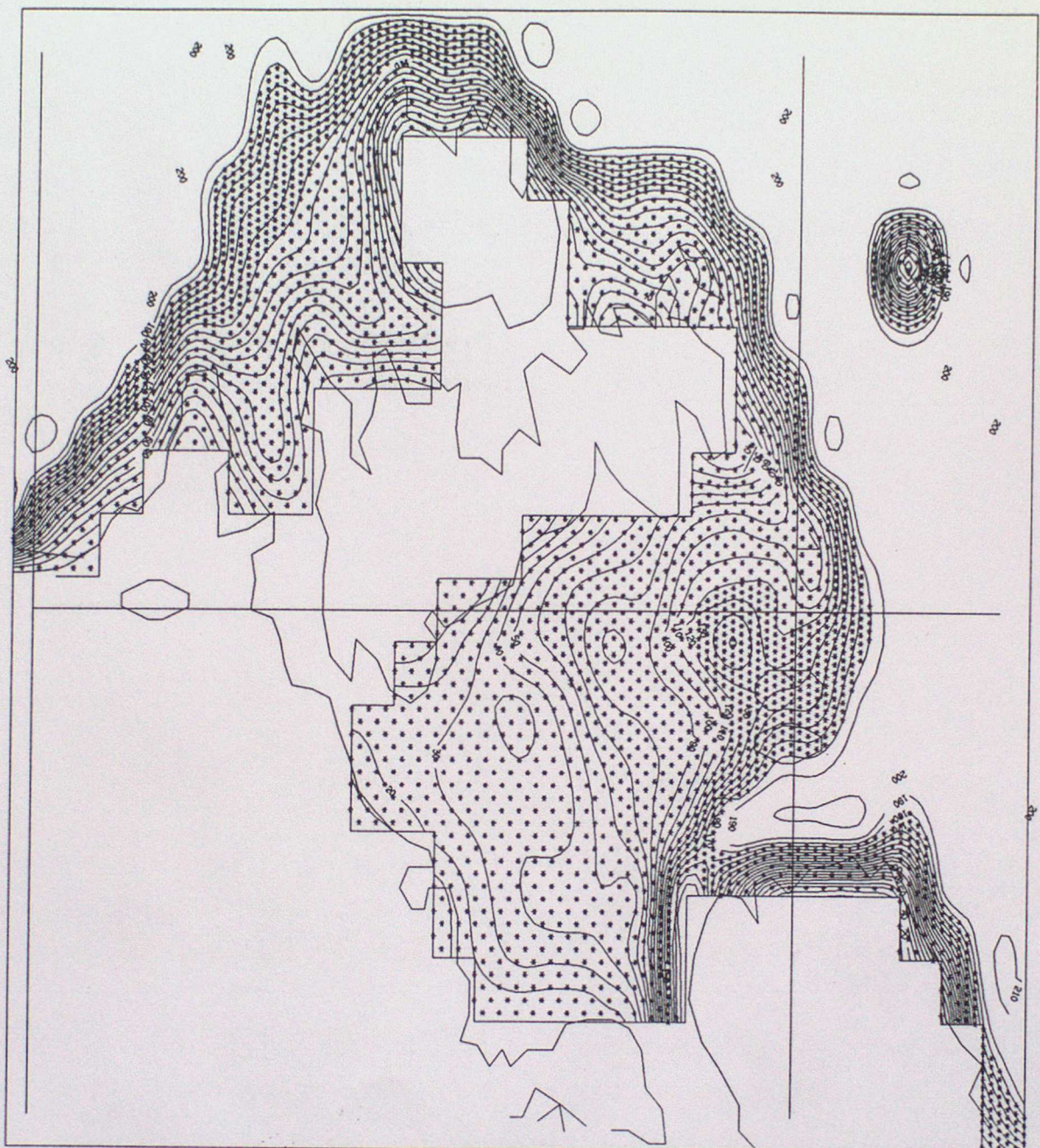


Figure 2b

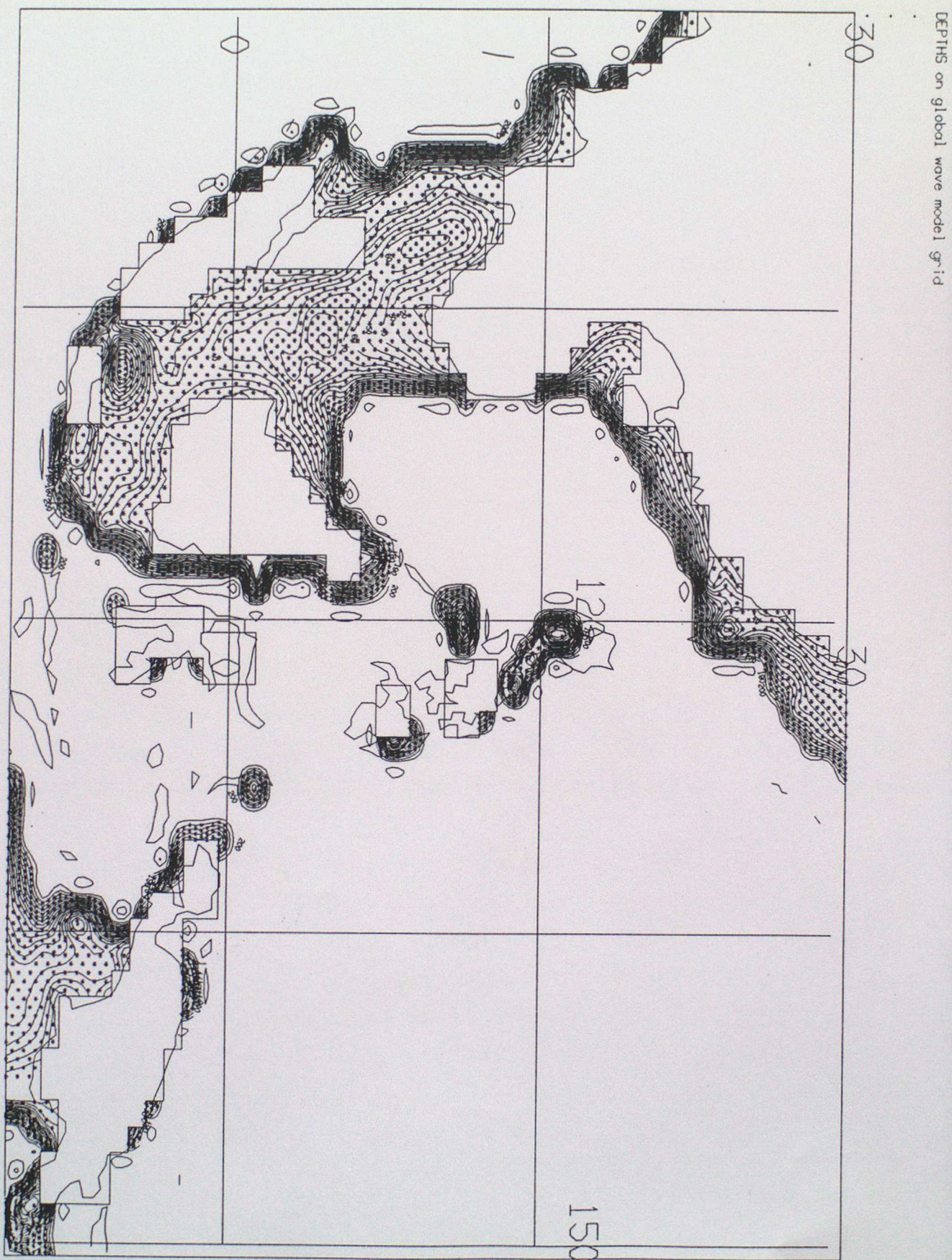


Figure 2c

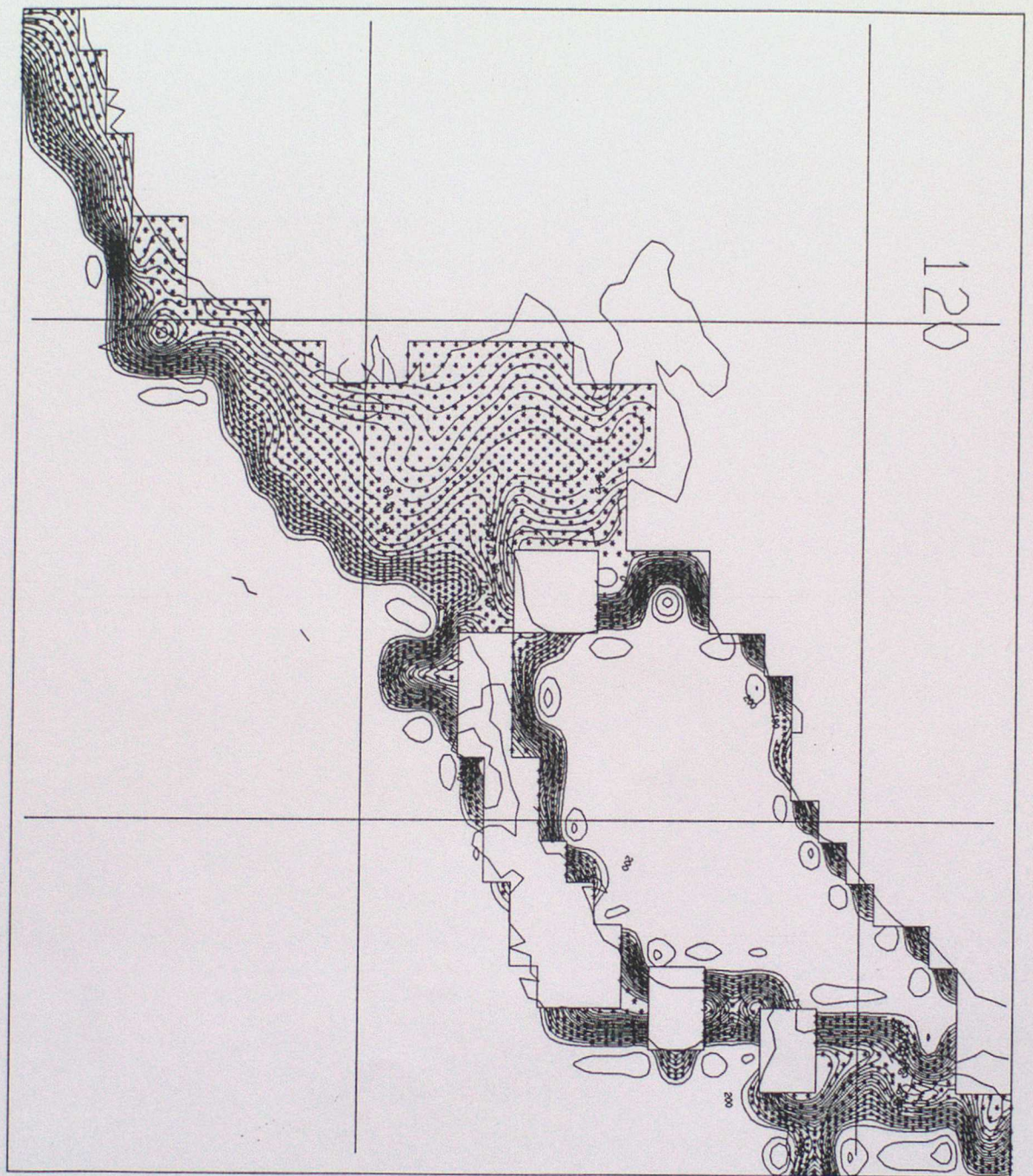


Figure 2d

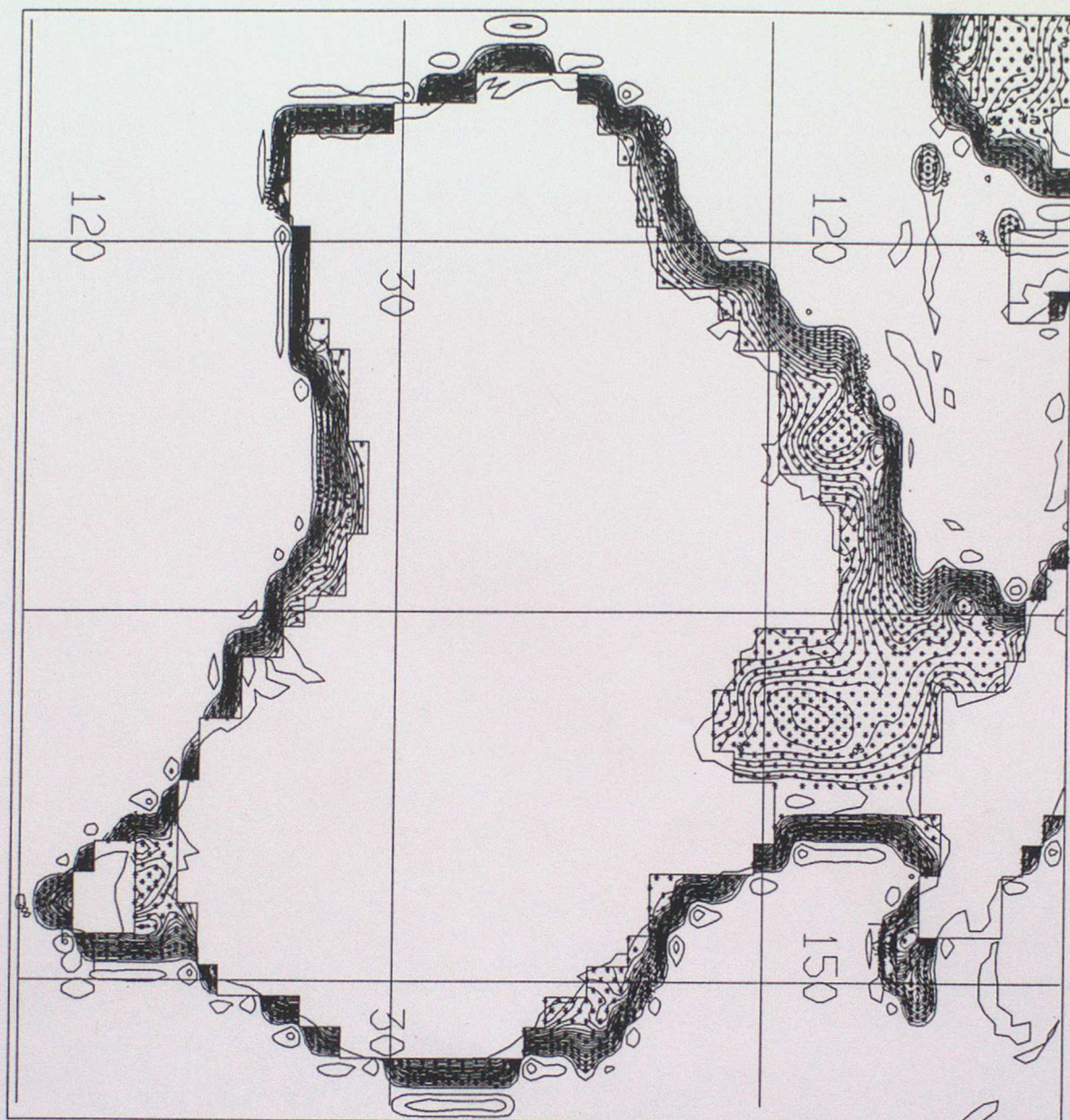


Figure 2e

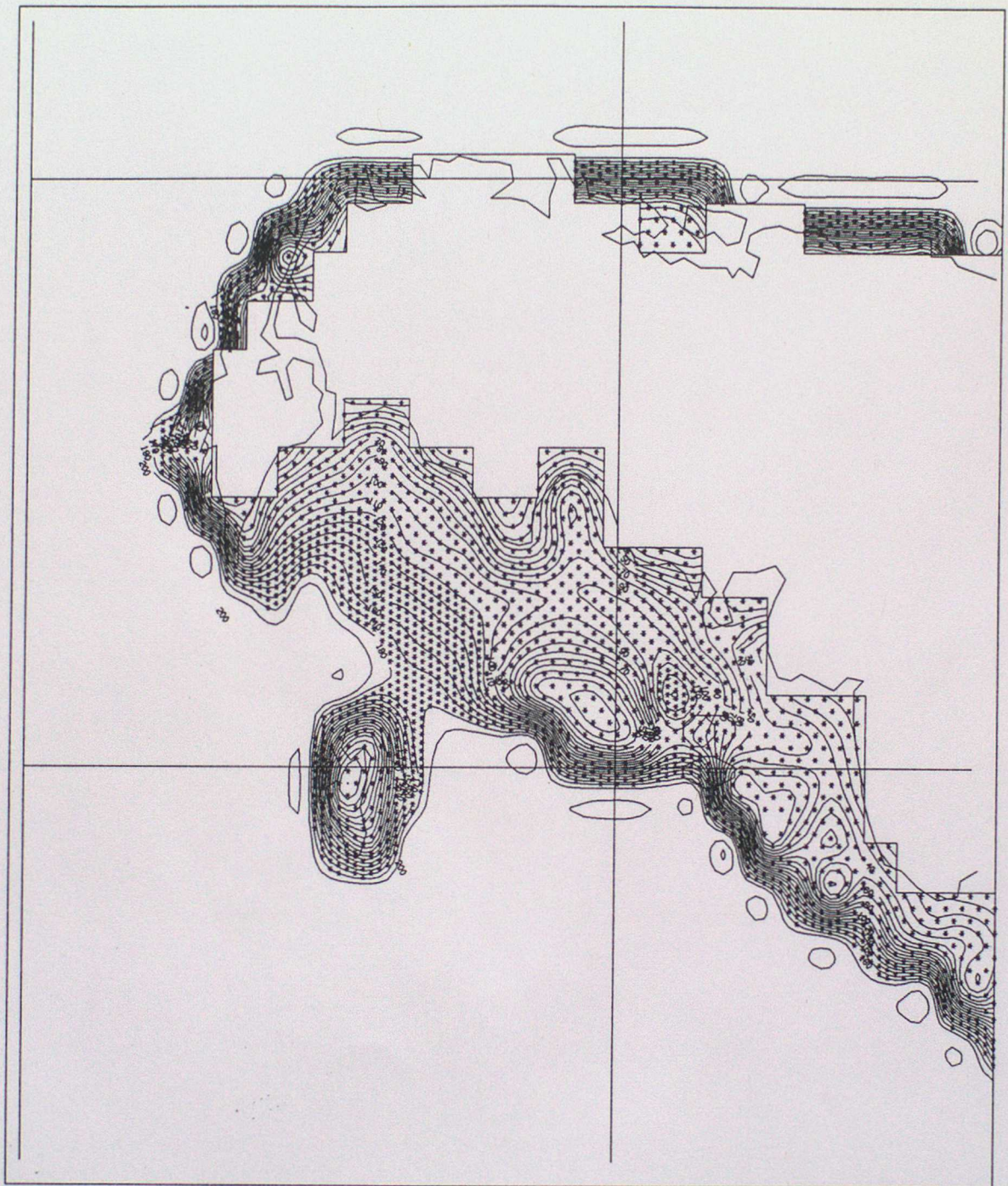


Figure 2f

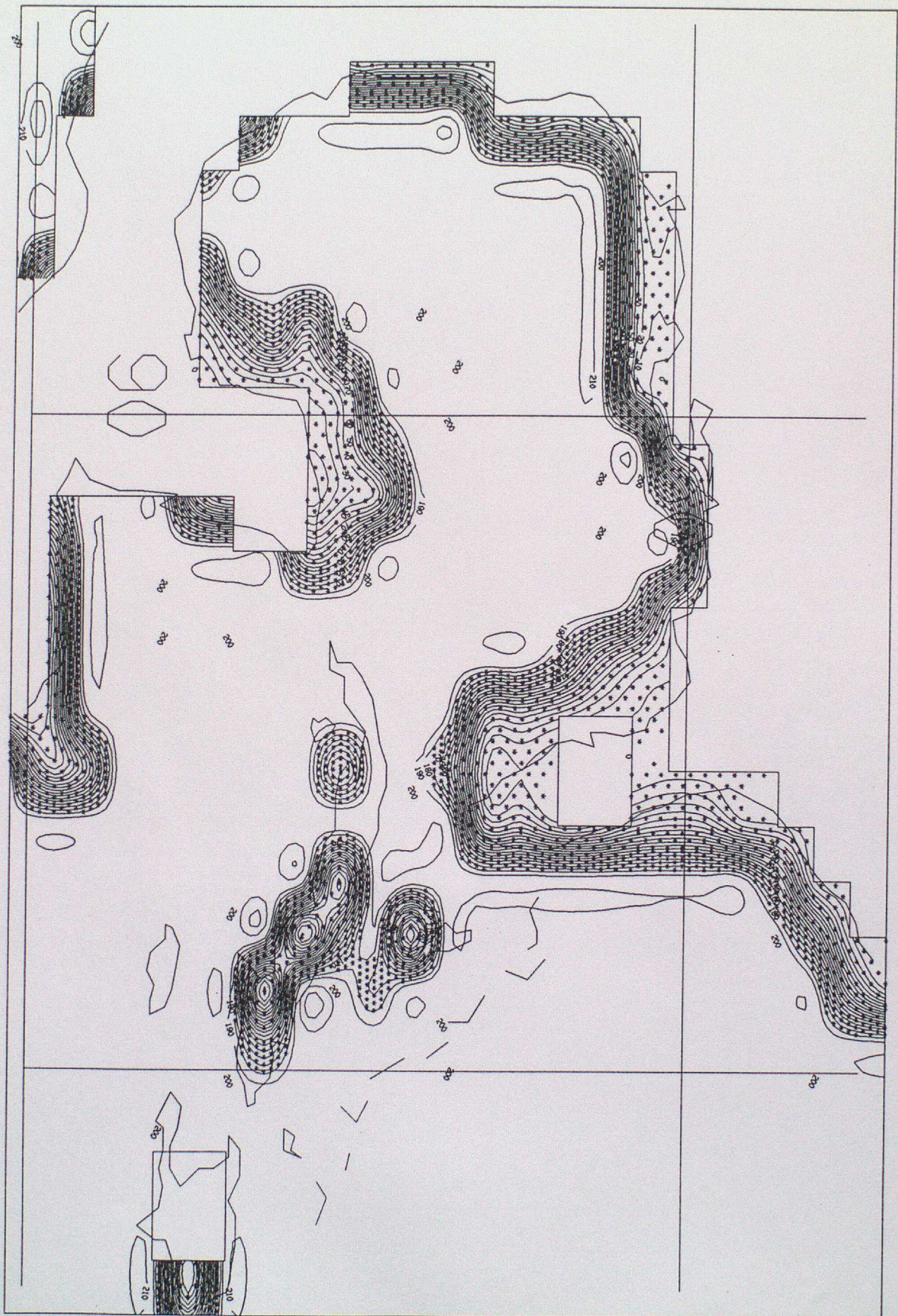


Figure 3 Depth at which waves of a given frequency start to feel the sea bottom

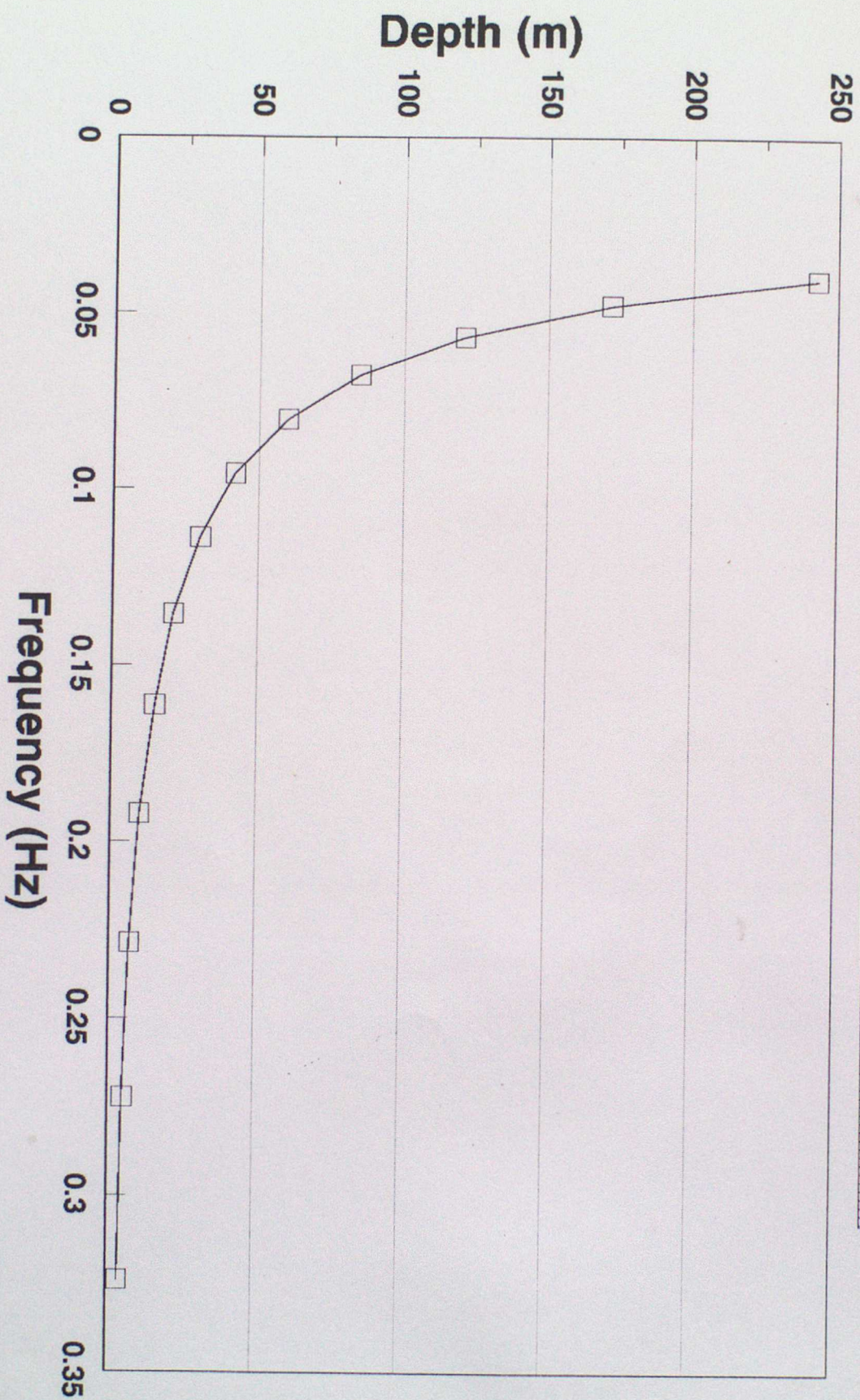
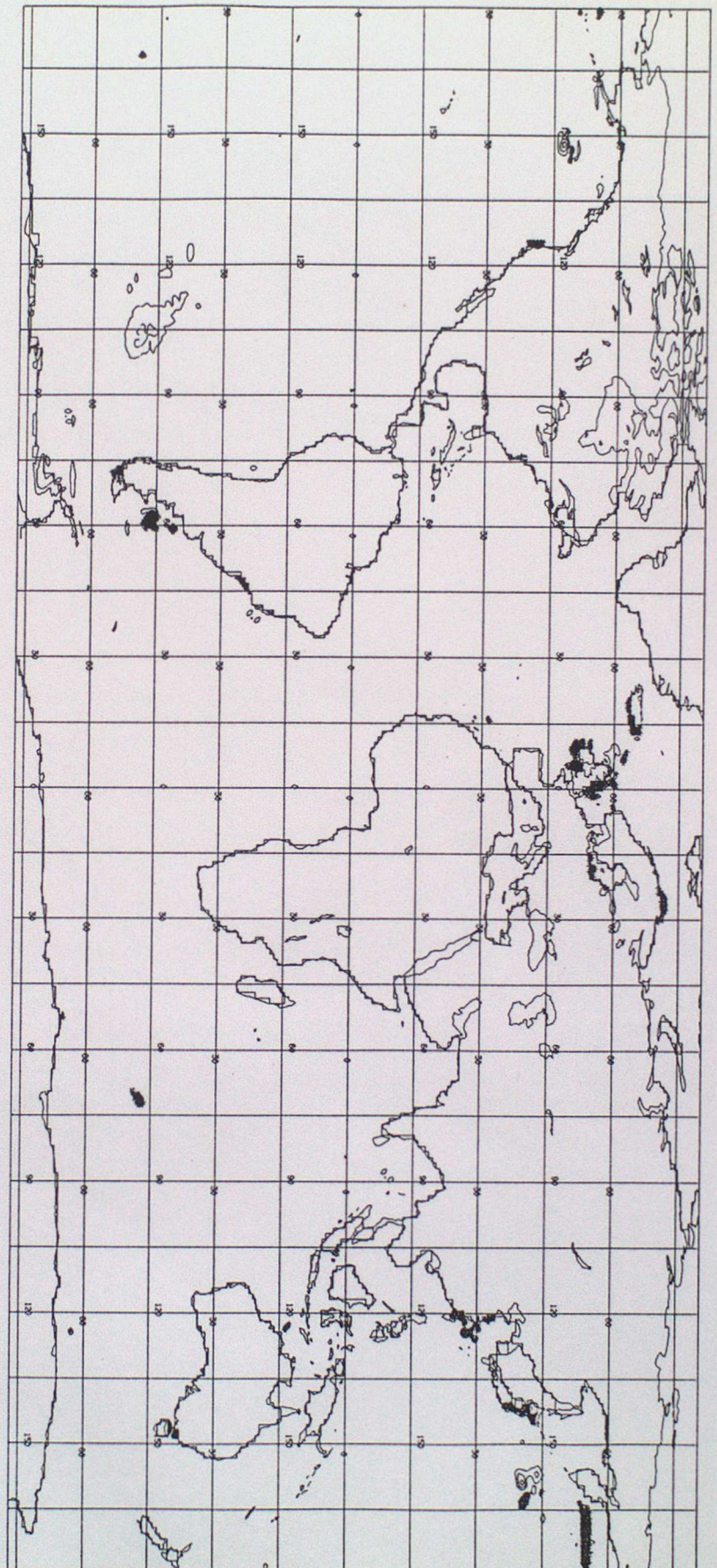
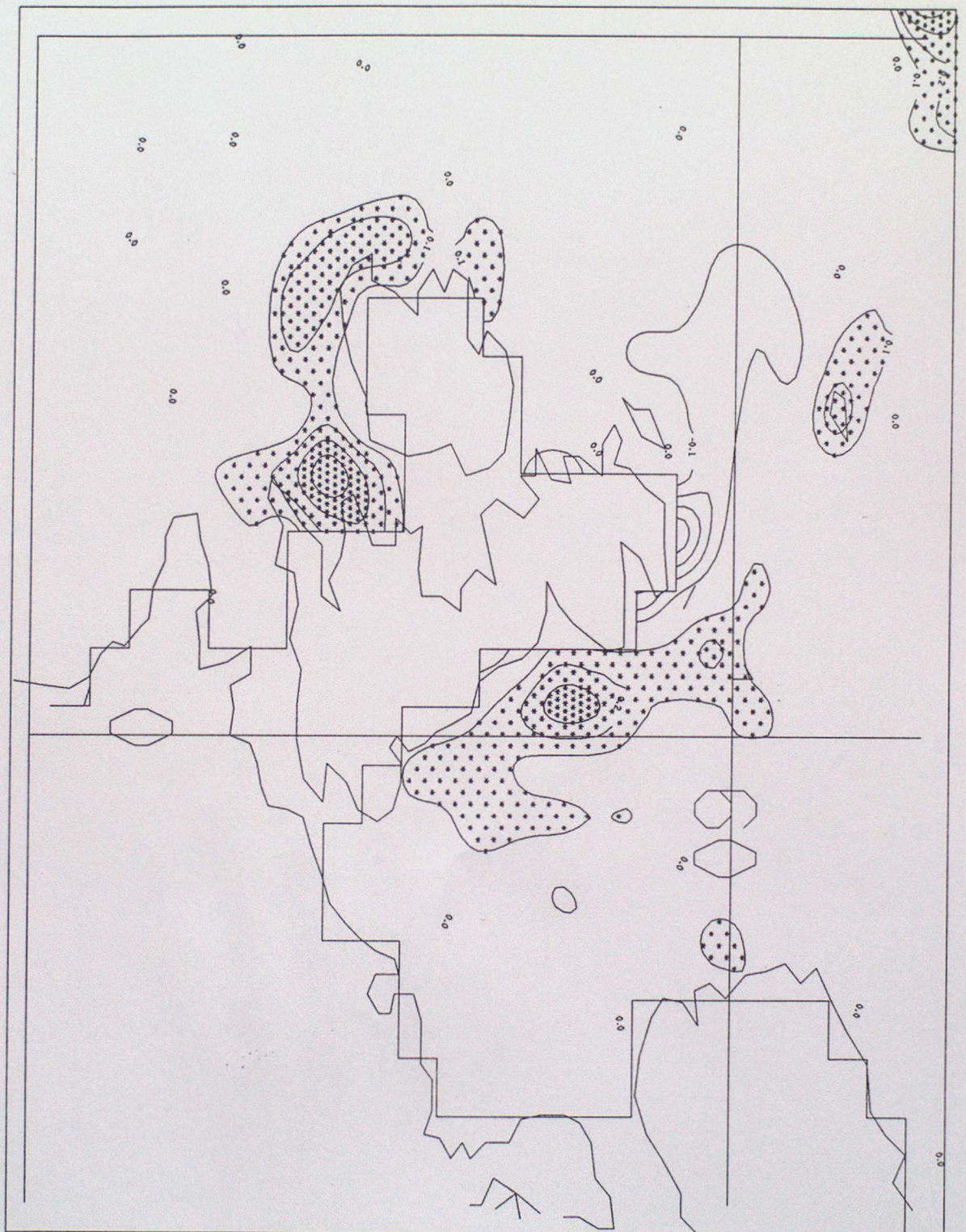


Figure 4



WAVE HEIGHT DIFFERENCE GLOBAL OPER - SHALLOW
VALID AT 12Z ON 30/3/1993 DATA TIME 12Z ON 30/3/1993

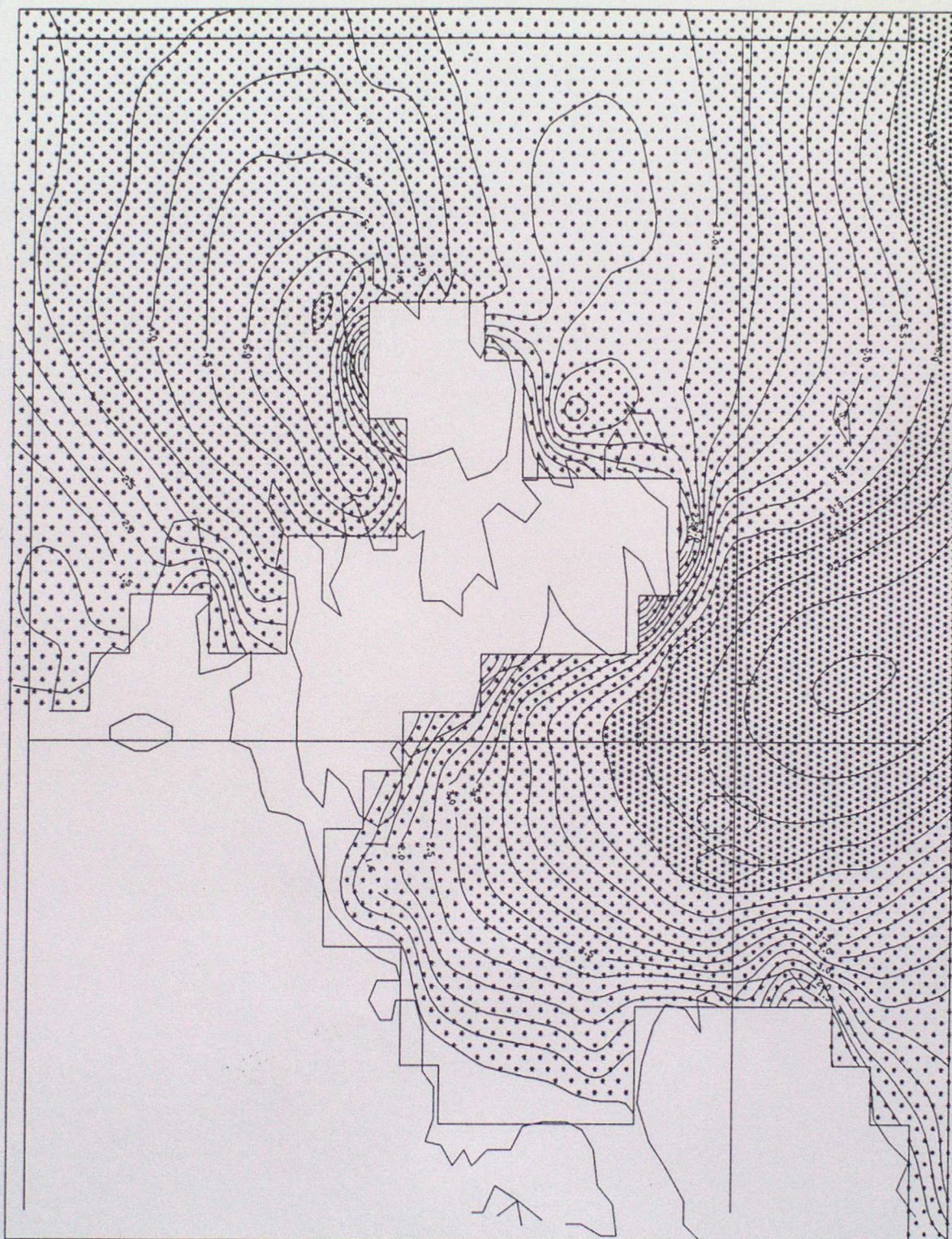
Figure 5a



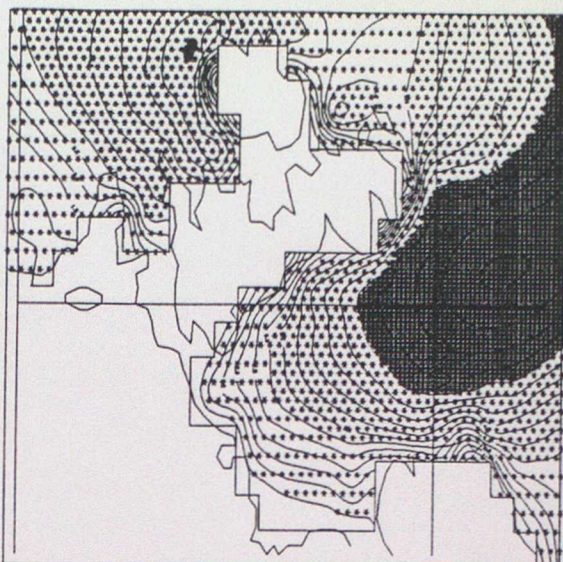
WAVE HEIGHT DIFFERENCE GLOBAL OPER - SHALLOW

VALID AT 12Z ON 30/3/1993 DATA TIME 12Z ON 30/3/1993

WAVE HEIGHT GLOBAL OPER
VALID AT 12Z ON 30/3/1993 DATA TIME 12Z ON 30/3/1993

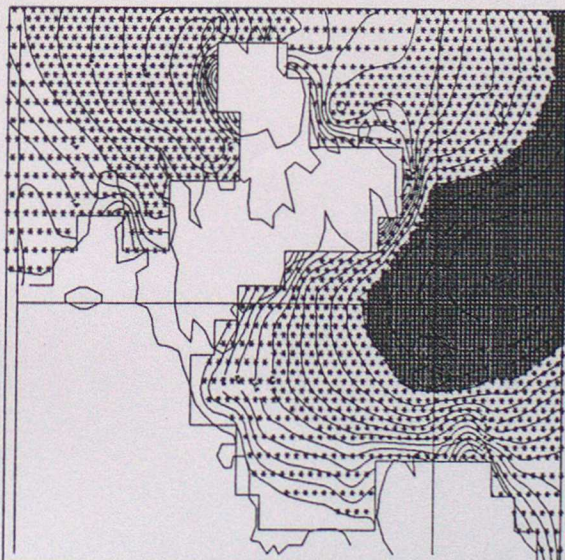


WAVE HEIGHT R.00M. 0758
 VALID AT 12Z ON 30/3/1993 DATA TIME 12Z ON 30/3/1993



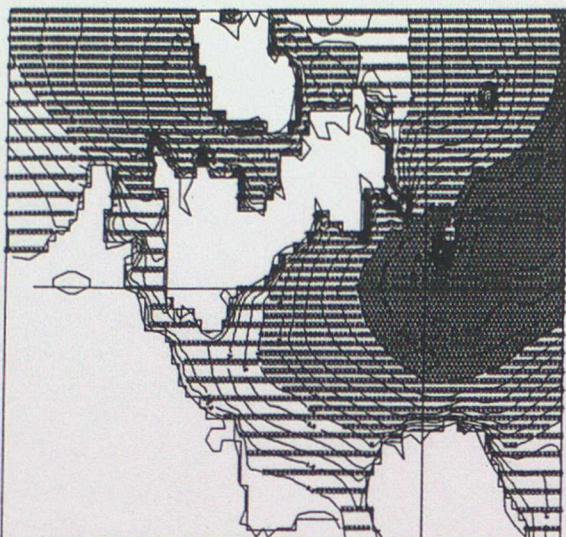
a)

WAVE HEIGHT R.00M. SHALLOW
 VALID AT 12Z ON 30/3/1993 DATA TIME 02 ON 30/3/1993



b)

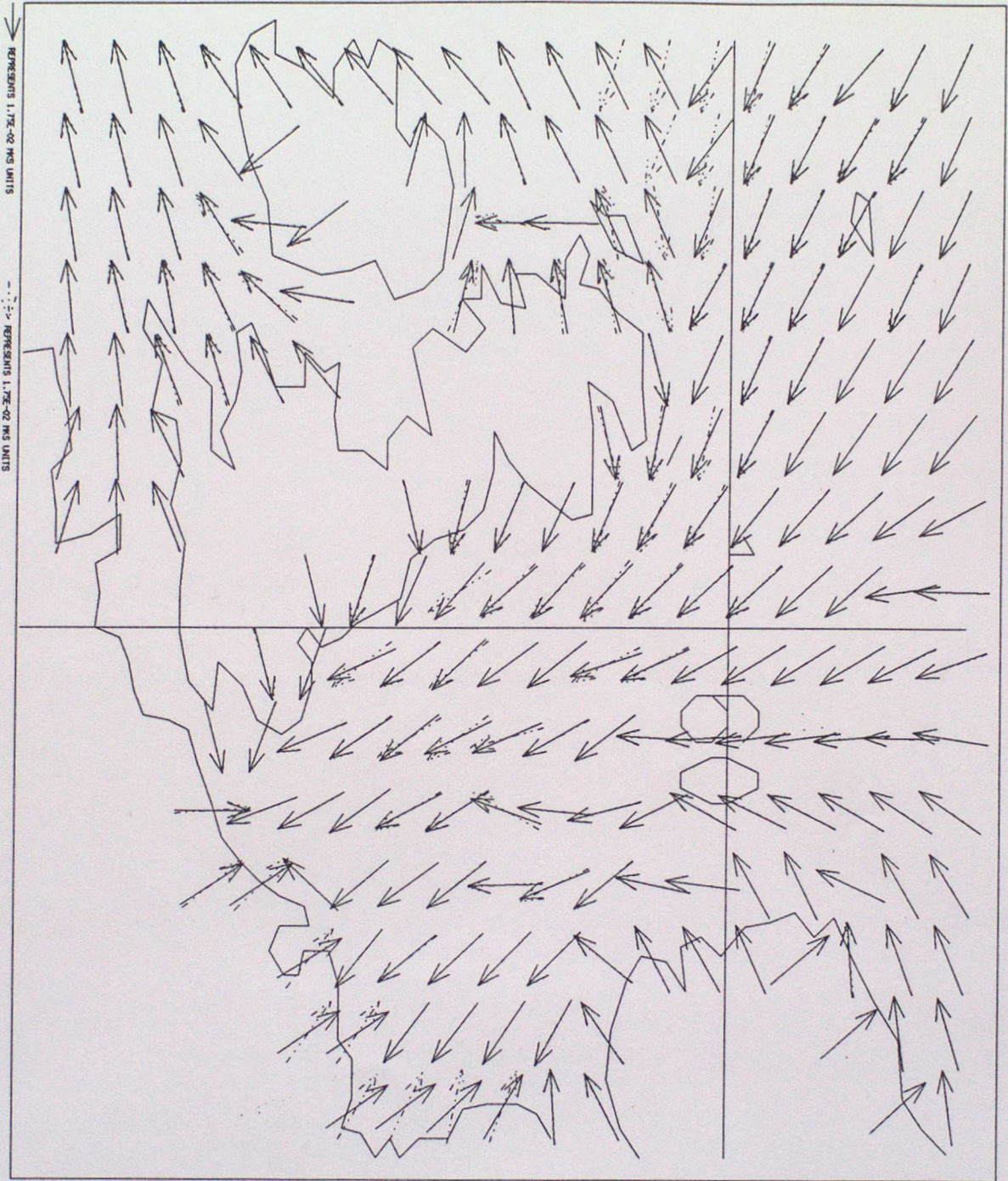
WAVE HEIGHT European model
 VALID AT 12Z ON 30/3/1993 DATA TIME 12Z ON 30/3/1993



c)

Figure 6

Figure 7



WAVE DIRECTION GLOBAL OPER (solid) GLOBAL SHALLOW (dashed)

VALID AT 12Z ON 30/3/1993 DATA TIME 12Z ON 30/3/1993

Figure 8

WAVE HEIGHT DIFFERENCE GLOBAL OPER - SHALLOW
VALID AT 12Z ON 30/3/1993 DATA TIME 12Z ON 30/3/1993

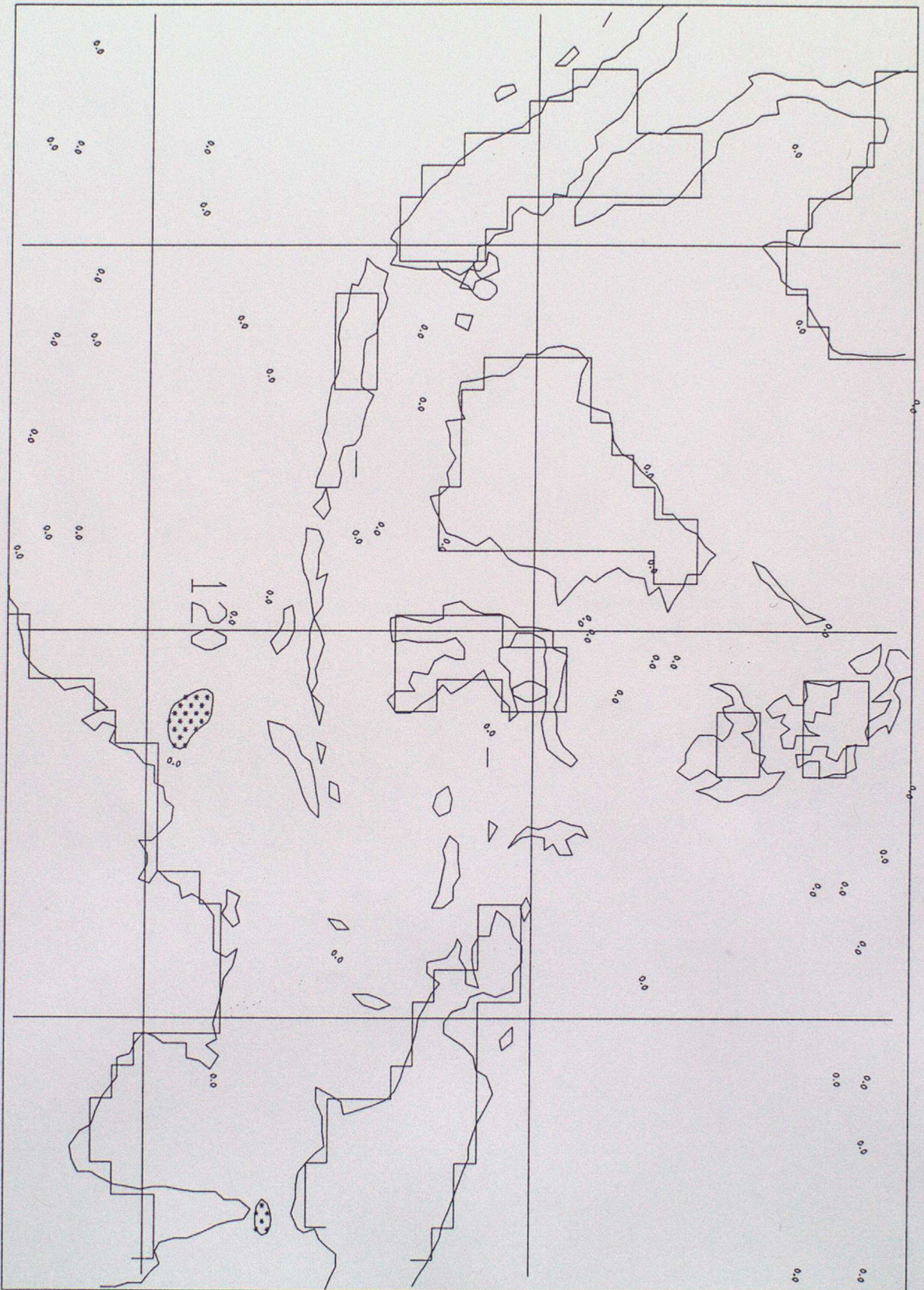
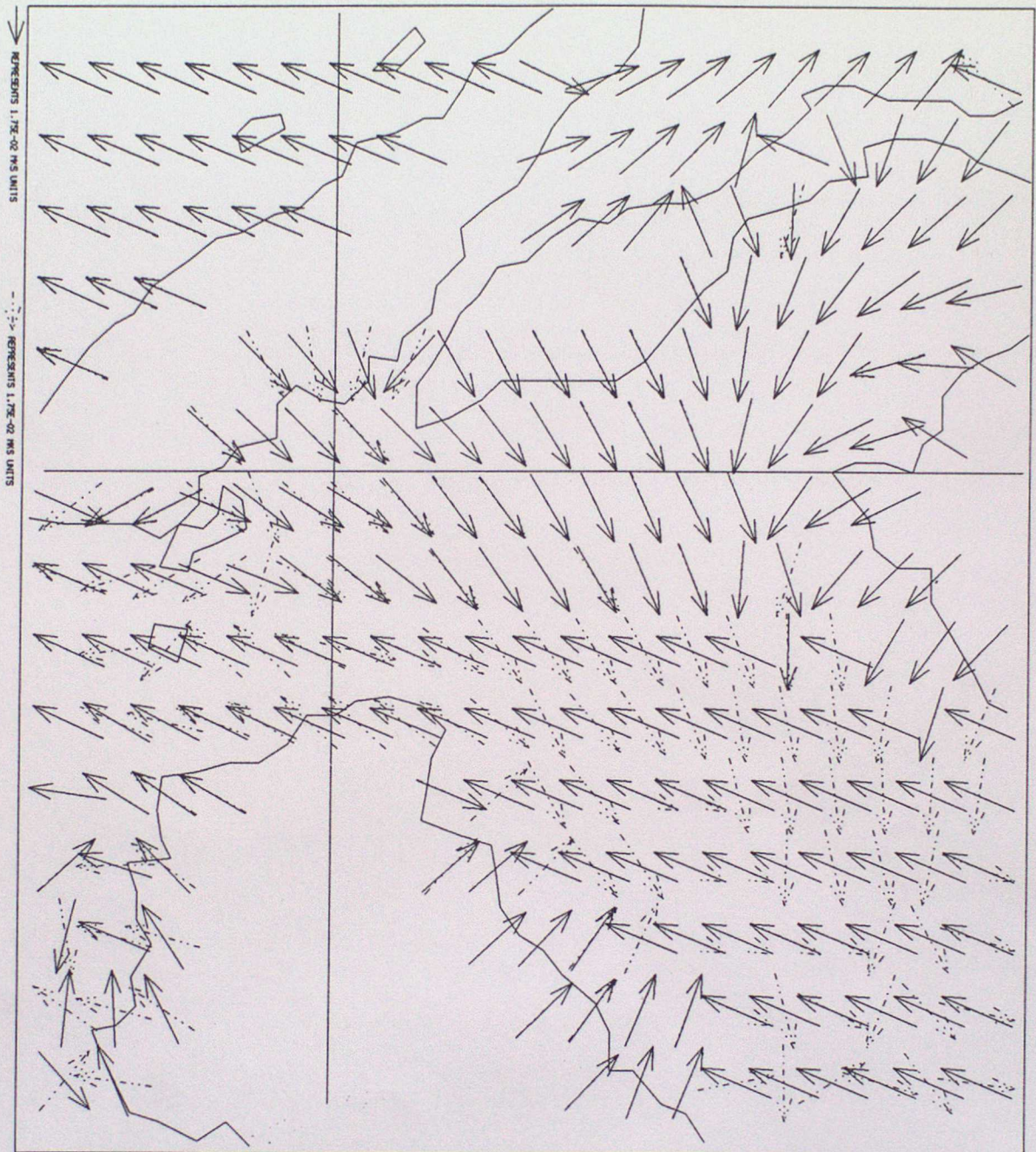


Figure 9



WAVE DIRECTION GLOBAL OPER (solid) GLOBAL SHALLOW (dashed)
VALID AT 12Z ON 30/3/1993 DATA TIME 12Z ON 30/3/1993

Forecasting Research Division Technical Reports

Forecasting Research Division Technical Reports

1. ON THE TIME SAVING THAT CAN BE ACHIEVED BY THE USE OF AN OPTIMISED COURSE IN AN AREA OF VARIABLE FLOW R.W. Lunnon
A.D. Marklow
September 1991
2. Treatment of bias in satellite sea surface temperature observations R.S.Bell
August 1991
3. FINITE DIFFERENCE METHODS M.J.P. Cullen
August 1991
4. Representation and recognition of convective cells using an object-orientated approach W.H. Hand
30th September 1991
5. Sea-ice data for the operational global model. C.P.Jones
November 1991.
6. Tuning and Performance of the Atmospheric Quality Control. N.B. Ingleby.
December 1991.
7. More satellite sounding data - can we make good use of it? R.S.Bell
January 1992.
8. WAM/UKMO Wind Wave model Intercomparison Summary Report Heinz Gunther
ECMWF
Martin Holt
UK Met Office
January 1992
9. Spin up problems of the UKMO Mesoscale Model and moisture nudging experiments Akihide Segami
JMA
February 1992
10. A comparison of 2nd generation and 3rd generation wave model physics M.W. Holt
B.J. Hall
February 1992
11. RETRIEVAL AND ASSIMILATION: SYSTEM CONSIDERATIONS Andrew C Lorenc
March 1992
12. Detection of Precipitation by Radars in the UK Weather Radar Network M. Kitchen
P.M. Brown
April 1992
13. THE VALUE OF WIND OBSERVATIONS FOR WEATHER FORECASTING AND CLIMATE STUDIES Andrew C Lorenc
April 1992
14. An investigation into the parameters used in the analysis scheme of the Mesoscale Model G. Veitch
B.J. Wright
S.P Ballard
May 1992
15. THE VERIFICATION OF MESOSCALE MODEL FORECASTS OF LIQUID WATER CONTENT USING HELICOPTER REPORTS OVER THE NORTH SEA DURING WINTER 1991 M. Ahmed
R.W Lunnon
R.J. Graham
May 1992

Forecasting Research Division Technical Reports

- | | | |
|-----|---|---|
| 16. | Simulations of the Diurnal Evolution of Marine Stratocumulus Part I: The sensitivity of the Single Column Version of the Mesoscale Model to Changes in the Turbulence Scheme. | S.D.Jackson
S.P. Ballard
May 1992 |
| 17. | Simulations of the Diurnal Evolution of Marine Stratocumulus Part II: A Comparison of Radiation Schemes Using the Single Column Version of the Mesoscale Model. | S.D.Jackson
S.P. Ballard
May 1992 |
| 18. | Quantifying the low level windshear aviation hazard for the UK: some research proposals | R.J. Graham
R.W. Lunnon
May 1992 |
| 19. | WAM/UKMO Wind Wave model Intercomparison Part 2
Running the UKMO wave model at higher resolution | M.W. Holt
April 1992 |
| 20. | Sensitivity of Mesoscale Model forecasts of anticyclonic Stratocumulus to the specifications of initial conditions and Boundary Layer mixing scheme. | B.J. Wright
S.P. Ballard
July 1992 |
| 21. | Evaluation of diffusion and gravity wave changes in the Global Forecast Model. | F. Rawlins
O. Hammon
16 June 1992 |
| 22. | Background Errors for the Quality Control and Assimilation of Atmospheric Observations in the Unified Model - the situation in July 1992. | C.A. Parrett
July 1992 |
| 23. | Estimation of the Mean and Standard Deviation of the Random Component of Data also Containing Non- random Errors. | B.R. Barwell
July 1992 |
| 24. | Experiments in Nowcasting convective rain using an object- oriented approach. | W.H. Hand
15th August
1992 |
| 25. | Gravity Wave Speeds from the Eigenmodes of the Unified Model. | I. Roulstone
28 July 1992 |
| 26. | A re-calibration of the Wave Model | M.W. Holt
August 1992 |
| 27. | Evaluation of Koistinen's method of radar range and bright band correction | A.G. Davies
August 1992 |
| 28. | A Study of the Boundary Layer in the Mesoscale Unified Model | Graham Veitch
August 21, 1992 |
| 29. | Profiles of wind using time-sequences of absorption channel imagery from geostationary satellites: proof of concept using synthetic radiances | R.W. Lunnon
September 1992 |
| 30. | AN EMPIRICAL INVESTIGATION OF THE "WATER VAPOUR TEMPERATURE LAPSE-RATE FEEDBACK" TO THE GREENHOUSE EFFECT | K.F.A. Smith
R.J. Allam
J.S. Foot
September 1992 |
| 31. | Observation needs for operational ocean modelling | S.J. Foreman
September 1992 |

Forecasting Research Division Technical Reports

- | | | |
|-----|---|---|
| 32. | Bright band correlations for layered precipitation; the comparison of Chilbolton radar data and Hardaker model output. | A.G. Davies
November 1992 |
| 33. | Progress and performance of the operational mesoscale model | S.P. Ballard |
| 34. | Assessment of the bias of significant wave height in the Met.Office global wave model | S.J. Foreman
M.W. Holt
S. Kelsall |
| 35. | STUDY OF CIRRUS CLOUD WINDS: ANALYSIS OF I.C.E DATA
FINAL REPORT FOR EUMETSAT CONTRACT ITT 91/16 | R.W. Lunn
D.A. Lowe
J.A. Barnes
I. Dharssi
December 1992 |
| 36. | Revisions to the operational data assimilation-Nov.92 | R.S. Bell
January 1993 |
| 37. | A comparison of wind observations from a flight of the DRA(B)BAC 1-11 research aircraft over Hemsby, 11 June 1991, with observations from the Hemsby radiosonde | R.J. Graham
January 1993 |
| 38. | The Moisture Observation Pre-processing System | B.J. Wright
January 1993 |
| 39. | Performance of the data assimilation scheme in the operational trial of the new mesoscale model. | B. Macpherson
B.J. Wright
A.J. Maycock
January 1993 |
| 40. | Development and performance of the new mesoscale model. | S.P. Ballard
B. Robinson
January 1993 |
| 41. | A PRELIMINARY ASSESSMENT OF OCEAN SURFACE FLUXES FROM UNIFIED MODEL FORECASTS | J.O.S. Alves
S.J. Foreman
M.W. Holt
S. Kelsall
S.J. Nightingale
January 1993 |
| 42. | Some notes on primitive and quasi-equilibrium equations with a hybrid vertical coordinate and remarks on Hamiltonian structure. | I. Roulstone
23rd March 1993 |
| 43. | Development of the surface data assimilation scheme for the new mesoscale model | A.J. Maycock
April 1993 |
| 44. | A REVIEW OF SEA ICE MODELS FOR USE IN FOAM | C.G. Sherlock
April 1993 |
| 45. | Running the global wave model with shallow water depth information. | M.W. Holt
April 1993 |